# ADVANCES IN FINITE ELEMENT TECHNIQUES

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# Edited by M. Papadrakakis and B.H.V. Topping



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#### **\*PREFACE**\*

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Manolis Papadrakakis and Barry Topping July 1994