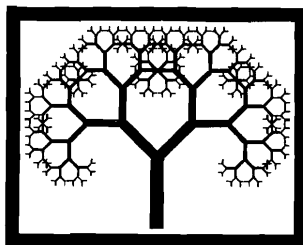


**ADVANCES
IN
NON-LINEAR
FINITE ELEMENT METHODS**

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*Edited by
B.H.V. Topping and M. Papadrakakis*



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❖PREFACE❖

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Barry Topping and Manolis Papadrakakis
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